

**4<sup>th</sup> Semester (B.Sc.-H) Final Internal Examination-2020**

**Department of Physics  
Prabhat Kumar College, Contai  
Paper-C8 (Mathematical Physics III)**

**Group-A (Theory)**

(Answer any one of the following)

1. Derive the Cauchy-Riemann equations in connection with analyticity as a function of complex variables. Find their forms in polar form also.
2. Define singularity of a function of the complex variable. Discuss various types of singularities.
3. Establish Cauchy Integral theorem. Evaluate  $\oint \frac{dz}{z}$  along a closed path C (i) not encircling the origin and (ii) encircling the origin.
4. Define Fourier and Inverse Fourier transforms. Find Fourier transform of the Delta function,  $\delta(x - a)$ . Calculate the Fourier transform of the function  $f(x)\cos(ax)$ .
5. Define Symmetric and Skew-Symmetric matrices, Hermitian and Skew- Hermitian matrices. Find all eigenvalues and corresponding eigenvectors for the matrix  $A = \begin{bmatrix} 2 & -3 & 0 \\ 2 & -5 & 0 \\ 0 & 0 & 3 \end{bmatrix}$ .
6. Define orthogonal and unitary matrices. Find the characteristic equation of the matrix  $A = \begin{bmatrix} 1 & 4 \\ 2 & 3 \end{bmatrix}$ . Applying the Cayley-Hamilton theorem calculate the Inverse of A.

**Group-B (Practical)**

(Answer any one of the following)

1. Write a program in python to find the inverse of the following matrix,  $A = \begin{bmatrix} 3 & 5 & 8 \\ 4 & 6 & 9 \\ 8 & 6 & 4 \end{bmatrix}$ .
2. Find the best fit straight line using least square fitting corresponding to the following data:

x	1	3	5	7	9
Y	10.7	13.1	15.2	17.6	19.9
3. Compute the value of integration  $\int \sqrt{x}e^{-x}dx$  using scipy module.
4. Write a program to compute the value of resistance (R) from the five set of data of Ohm's law experiment with relevant plot.

V (Volt)	2.1	3.2	3.8	4.5	4.8
I (mA)	5.12	7.80	9.26	10.90	11.70
5. Write a program to find the solution of the three given linear equations:  
 $3x + 2y + 4z = 7$ ,  $2x + y + z = 4$ ; and  $x + 3y + 5z = 2$ .
6. Write a python program to solve the differential equation for radioactive decay using Euler method and plot it using Matplotlib module.

**Answer script submitted to [ppcontai@gmail.com](mailto:ppcontai@gmail.com)**